Reading Questions 13

page 156: example 7

1. The matrix $\begin{bmatrix} 3 & 0 \\ 0 & 2 \end{bmatrix}$ is similar to the matrix $\begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix}$. 2. If $\begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix}$ is similar $\begin{bmatrix} 2 & 1 \\ 0 & 1 \end{bmatrix}$ then $\begin{bmatrix} 4 & 0 \\ 0 & 1 \end{bmatrix}$ is similar to $\begin{bmatrix} 4 & 2 \\ 0 & 1 \end{bmatrix}$. 3. Suppose $A = SBS^{-1}$ where $A = \begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix}$. What is B?

Section 3.4 Coordinates (Part 2)

The coordinate vector

P 1. Write down what it means for two matrices to be similar.

P 2. If A is similar to the identity matrix what can you say about A?

P 3. Let

$$A = \begin{bmatrix} 2 & 0 \\ 0 & 3 \end{bmatrix} \quad \text{and} \quad B = \begin{bmatrix} 2 & 1 \\ 0 & 3 \end{bmatrix}.$$

Find an invertible matrix S such that AS = SB.

P 4. Suppose
$$\begin{bmatrix} 1 & 2 \\ 4 & 3 \end{bmatrix} = S \begin{bmatrix} 5 & 0 \\ 0 & -1 \end{bmatrix} S^{-1}$$
. Find a matrix *C* which is similar to $\begin{bmatrix} 9 & 8 \\ 16 & 17 \end{bmatrix}$.